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BOUNDARY-LAYER CHARACTERISTICS AT MACH NUMBERS 2 THROUGH 5 IN THE TEST SECTION OF THE 12-INCH SUPERSONIC TUNNEL (D)

Ву

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D. R. Beil von Kármán Gas Dynamics Facility ARO, Inc.

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BOUNDARY-LAYER CHARACTERISTICS AT MACH NUMBERS 2 THROUGH 5 IN THE TEST SECTION OF THE 12-INCH SUPERSONIC TUNNEL (D)

Ву

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September 1963 ARO Project No. VD2257

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ABSTRACT

As part of a general tunnel calibration program, an investigation was made of the boundary-layer characteristics at Mach numbers 2, 3, 4, and 5 in the test section of the 12-Inch Supersonic Tunnel (D). The boundary-layer measurements were made at one longitudinal station (near the pitch sector center of rotation) on the centerline of both the flexible plate and sidewall. Measurements were also made at vertical locations on the sidewall between the sidewall centerline and the upper

The boundary-layer total thickness, displac momentum thickness are presented at each Mach number over a Reynolds number range corresponding, in general, to tunnel stagnation pressures between 5 and 60 psia. At each Mach number, the variation of displacement thickness on the sidewall between the centerline and the upper flexible plate is presented as is a correlation of the flexible plate displacement thickness with experimental data obtained in other wind tunnels. Velocity profiles and test section Mach numbers are presented to indicate variations with Reynolds number.

PUBLICATION REVIEW

This report has been reviewed and publication is approved.

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NOMENCLATURE

- a_o Speed of sound at stagnation conditions, ft/sec
- g Ratio of boundary-layer displacement thickness to total thickness, δ*/δ
- H Ratio of boundary-layer displacement thickness to momentum thickness, $\delta*/\theta$
- K 0.0131 $\left(\frac{\mu_0}{\rho_0 n_0}\right)^{\frac{1}{2}}$
- M_m Free-stream Mach number
- 11 /11 1.../21/N
- Po tumer oragination probate, rea-
- Re Test section unit Reynolds number
- Uy Local velocity within the boundary layer at distance y from wall. ft/sec
- U_m Free-stream velocity, ft/sec
- XE Longitudinal distance of the nozzle aerodynamic exit plane referenced to nozzle throat location, in.
- y Distance normal to wall, in.
- δ Boundary-layer total thickness, in.
- $\delta_{\rm L}$ Laminar sublayer thickness of the boundary layer, in.
- δ* Boundary-layer displacement thickness, $\int_{0}^{\delta} \left(1 \frac{\rho_{y} U_{y}}{\rho_{\infty} U_{\infty}}\right) dy$, in.
- δ^* Displacement thickness parameter, $\frac{\delta^*}{k x_E}$
- Boundary-layer total thickness, $\int_{0}^{\delta} \frac{\rho_{y} U_{y}}{\rho_{\infty} U_{\infty}} \left(1 \frac{U_{y}}{U_{\infty}}\right) dy$, in.
- $\mu_{\rm O}$ Coefficient of viscosity at stagnation conditions, lb sec/ft²
- $ho_{
 m O}$ Density at stagnation conditions, lb sec $^2/{\rm ft}^4$
- ρ_y Local density within the boundary layer at distance y from wall, lb $\text{sec}^{\,2}/\text{ft}^{\,4}$
- Free-stream density, 1b sec²/ft⁴

1.0 INTRODUCTION

A test program was conducted to calibrate, at the lower Reynolds numbers, the test section of the 12-Inch Supersonic Tunnel (D) of the von Karman Gas Dynamics Facility (VKF), Arnold Engineering Development Center (AEDC), Air Force Systems Command (AFSC). As part of this calibration program the boundary-layer characteristics on the flexible plate and sidewall of the tunnel test section were obtained over the Reynolds number range from 0.02 to 0.69 x 10⁶ per inch at Mach numbers 2, 3, 4, and 5. This report presents the results of the boundary-layer investigation and convolutes the flexible plate displacement thickness.

2.0 APPARATUS

2.1 WIND TUNNEL

The 12-Inch Supersonic Tunnel (D) (Fig. 1) is an intermittent, variable density wind tunnel with a manually adjusted, flexible-plate-type nozzle. The tunnel operates at Mach numbers from 1.5 to 5 at stagnation pressures from about 5 to 60 psia and at stagnation temperatures up to about 90°F. A detailed description of the tunnel is given in Ref. 1.

2.2 INSTRUMENTATION

The pressure data from the boundary-layer rake was measured with a "trapped" reference system. This system used a 5- or 30-psid transducer (referenced to a vacuum) to measure a reference pressure obtained from the outermost rake probe. When the reference pressure reached a desired level, a valve was closed, sealing the reference from the probe pressure; hence, "trapped" reference. The pressure differential existing between the rake probes and the trapped reference was then measured with either a 1- or 15-psid transducer.

The boundary-layer parameters, δ , δ *, and θ were determined by methods and equations given in Ref. 2. The data was reduced by the VKF ERA 1102 computer.

Manuscript received August 1963.

The estimated maximum uncertainties of the boundary-layer thickness values presented are: total thickness, 7 percent; displacement thickness, 3 percent; and momentum thickness, 3 percent.

3.0 PROCEDURE

Boundary-layer measurements were made at one longitudinal station (near the pitch sector center of rotation) on the centerline of both the flexible plate and sidewall and at one-inch increments on the sidewall between the sidewall centerline and the upper flexible plate. Figure 2 presents a perspective drawing of the tunnel test section showing the various locations of the boundary-layer rake.

Although tests were made at Mach numbers 2, 3, 4, and 5 over the Reynolds number range of the tunnel, primary emphasis was placed on Reynolds numbers corresponding to stagnation pressures between 5 and 30 psia. Table 1 lists the specific condition at which measurements were made.

4.0 RESULTS AND DISCUSSION

Figure 3 shows a comparison of the theoretical values of the turbulent boundary-layer parameters, $g = \delta * / \delta$, and $H = \delta * / \theta$ obtained from Ref. 3, with the experimental values measured on the sidewall and flexible plate centerlines. The number beside each data point represents the experimental value of the velocity profile parameter N. The sidewall data are not presented at Mach numbers 4 and 5 because the experimental values of N were below the minimum value of 5 presented in Ref. 3. These lower values of N are characteristic of a laminar boundary layer.

The experimental values agree with theory at all Mach numbers presented with the exception of some values of the shape parameter H on the flexible plate centerline at Mach numbers 4 and 5. Those points which do not agree with the theory (N = 7.1, 8.3, and 10 at Mach 5 and N = 14 at Mach 4) are associated with the thicker laminar sublayers shown in the velocity profiles of Fig. 4 where the flow is becoming transitional in nature. This figure presents the boundary-layer velocity profile at Mach 4 and 5 in terms of the dimensionless parameter y/δ . The flexible plate boundary layer is characterized by a turbulent 1/N-power profile in its outer portion but has, at the lower Reynolds numbers, a relatively thick laminar sublayer represented by the linear fairing in the region adjacent to the wall (Ref. 4). The

sidewall centerline boundary layer exhibits laminar characteristics to the extent that its power profile parameter N is less than 5 at Mach 4 and 5; however, as the Reynolds number is increased, the value of N also increases as expected.

The flexible plate velocity profiles at the extremes of the Reynolds number ranges investigated (see Fig. 5) have been omitted from Fig. 4 because in their turbulent portions they are practically congruent with the N=7 profiles shown. The sidewall profiles at the intermediate Reynolds numbers have been omitted since they fall between the extremes shown.

Figure 5 presents the variation with Reynolds number of the boundarylayer total thickness &, displacement thickness &*, and momentum thickness heta on the flexible plate and sidewall centerlines. The increase in boundarylayer thickness δ , δ *, and θ on the flexible plate between Reynolds numbers of 70 and 100 thousand per inch at Mach 5 and 40 and 80 thousand per inch at Mach 4 is reflected in the variation of the test section Mach number with Reynolds number. Figure 6 shows the Mach number and flexible plate displacement thickness variations at Mach numbers 4 and 5. Changes of Mach number with Reynolds number are seen to be in a direction which would be produced by the variation of the boundary-layer thickness and in turn nozzle area ratio. Referring back to Fig. 4, it is also interesting to note that the turbulent outer portion of the flexible plate boundary layer is similar throughout the Reynolds number range with the exception of an increase in the velocity profile parameter, N, at the Reynolds number where the minimum displacement thickness was measured (Re/in. of 0.07 x 10^6 at Mach 5 and 0.040 x 10^6 at Mach 4).

In Fig. 7 the experimental values of the boundary-layer total and displacement thickness are compared with the theoretical values computed by the method of Tucker (Ref. 3). This method determines the turbulent boundary-layer development along an insulated surface with a pressure gradient. The theoretical skin friction coefficient used in the computations was calculated using an arithmetic-mean between the wall and stream temperature values for the viscosity calculations. Also a turbulent velocity profile parameter of N = 7 was assumed.

The flexible plate data presented for the maximum Reynolds number ($p_0 = 60$ psia) at Mach 2 and the minimum Reynolds number ($p_0 = 5$ psia) at Mach numbers 4 and 5 were obtained by a smooth curve extrapolation of the boundary-layer thickness variations with Reynolds number shown in Fig. 5.

Figure 8 shows the variation of the sidewall boundary-layer displacement thickness between the sidewall centerline and the upper flexible plate. The large decrease in displacement thickness as the top wall is approached at Mach 4 and 5, and to a lesser extent at Mach 3, is attributed to secondary cross-flows within the boundary layer. As discussed in Ref. 5, these cross-flows are the result of transverse static pressure gradients present in all non-axially symmetric nozzles.

Figure 9 presents a correlation of the displacement thickness measured on the flexible plate with experimental data measured in several other supersonic wind tunnels. This correlation is based upon a nondimensional displacement thickness parameter, δ^* .

where
$$\overline{\delta^*} = \frac{\delta^*}{KX_E^4/}$$
 and
$$K = 0.0131 \left(\frac{\mu_o}{\rho_o a_o}\right)^{1/2}$$

Reference 6 develops this relationship by rearranging the equations of Tucker (Ref. 3) to obtain a boundary-layer growth parameter independent of nozzle size and stagnation conditions.

In those instances where the position of the nozzle aerodynamic exit (location of last characteristic) is known, the experimentally determined values of $\delta*$ are transferred to this point before computing $\delta*$. This transfer is accomplished by the method of Ref. 6. Where the position of the aerodynamic exit is unknown, $\delta*$ is computed directly from the measured value of $\delta*$ and the distance from the throat to the point of measurement. Figure 9 indicates which method was used to compute the values of $\delta*$ shown.

Since Tucker's equations apply only to turbulent boundary-layer development, the tunnel D data which exhibited laminar sublayers are not included in Fig. 9. This figure shows that, for the most part, the tunnel D turbulent boundary-layer data correlates quite well with that of the other tunnels, although at Mach 4 and 5, values of δ * higher than the correlating values were obtained. At both of these Mach numbers, the high values of δ * occurred at the peak of a rapid increase in displacement thickness with Reynolds number (Re/in. = 0.10 x 10⁶ at Mach 5 and 0.000 x 10⁶ at Mach 4, Fig. 5) while the values of δ * which correlated best were obtained at the maximum Reynolds numbers tested.

5.0 SUMMARY

The following results were obtained from an investigation of the test section boundary-layer conducted in the 12-Inch Supersonic Tunnel (D) of the von Karman Gas Dynamics Facility:

- 1. With the exception of the sidewall centerline measurements at Mach 4 and 5, the test section boundary-layer characteristics were primarily turbulent.
- 2. The characteristics of the turbulent boundary layers agree well with theory except for the flexible plate boundary layers whose profiles exhibit well-defined laminar sublayers at Mach numbers 4 and 5. Here, the experimental values of H are higher than predicted by theory.
- 3. At Mach numbers 4 and 5, the variation of the test section Mach number with Reynolds number is associated with the variation of the flexible plate boundary-layer characteristics.
- 4. At Mach numbers 3, 4, and 5, the displacement thickness of the sidewall boundary layer decreases as the upper wall is approached. This decrease is attributed to secondary cross-flows within the boundary layer.
- 5. The flexible plate displacement thickness correlates with that of other supersonic wind tunnels when compared on the basis of the nondimensional parameter, δ^* .

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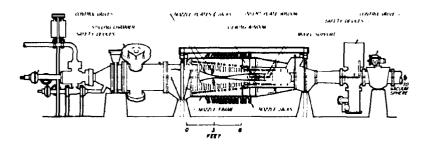
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TABLE 1
TEST CONDITIONS

| | | | | Sidewall | | | | | | |
|----------------|--------------------------|---------------------------|---------------------------|-----------------------|---|----|----|---|---|--|
| M _æ | p _o , psia | Re/in. x 10 ⁻⁶ | Flexible Plate Centerline | Distance above &, in. | | | | | | |
| | | | | £ | 1 | 2 | 3 | 4 | 5 | |
| 2 | 1 | 0. 02 | x | х | х | х | х | x | x | |
| | 5 | 0. 11 | × | х | x | × | × | x | x | |
| | 10 | 0.23 | x | х | x | x | х | х | x | |
| | 15 | 0.33 | x | x | x | x | x | х | x | |
| | 30 | 0.69 | × | × | x | x | × | x | x | |
| 3 | 5 | 0.07 | x | х | х | × | x | x | x | |
| | 10 | 0.14 | × | x | х | × | x | х | x | |
| | 15 | 0.21 | x | х | x | x | x | x | x | |
| | 20 | 0. 28 | x | x | x | x | х | x | | |
| | 30 | 0. 39 | | | | | | 1 | x | |
| | 60 | 0. 82 | × | х | x | х | × | x | x | |
| 4 | 5 | 0. 04 | x | х | x | × | x | х | | |
| | 10 | 0.08 | x | x | х | × | x | x | 1 | |
| | 15 | 0.12 | x | х | x | x | x | x | x | |
| | 20 | 0.16 | x | x | X | X. | х | | x | |
| | 60 | 0.48 | x | x | x | x | x | x | x | |
| 5 | 5 | 0.02 | x | | | | | | | |
| | 7 | 0.03 | x | x | | x | X. | x | 1 | |
| | 10 | 0.05 | x | x | x | x | x | x | | |
| | 15 | 0.07 | x | x | x | x | x | x | 1 | |
| | 17 | 0.08 | x | x | x | x | x | x | | |
| | 20 | 0.10 | x | × | x | | x | x | 1 | |
| | 30 | 0.14 | | x | х | | x | x | × | |
| | 40 | 0.19 | | | | | | | x | |
| | 60 | 0.29 | x | × | x | х | х | X | x | |

x Indicates where measurements were made



Assembly

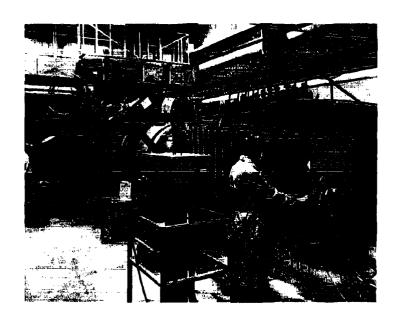


Fig. 1 The 12-inch Supersonic Tunnel (D)

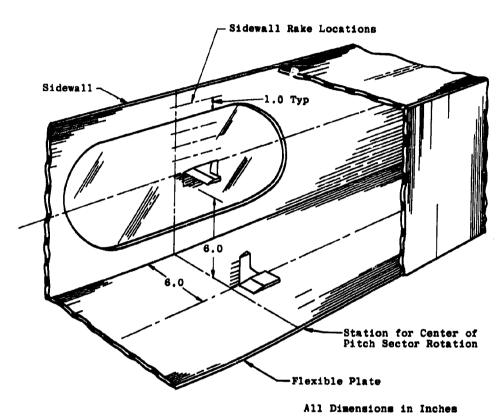


Fig. 2 Boundary-Layer Rake Locations

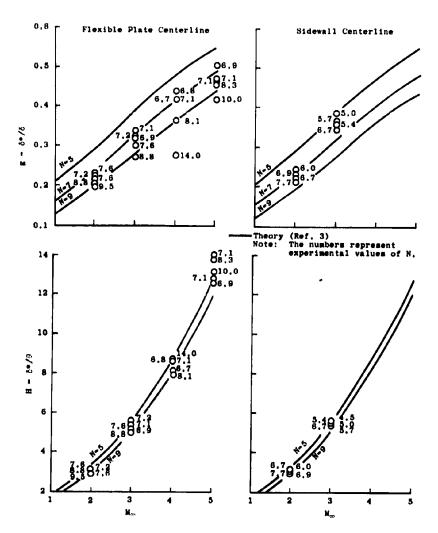


Fig. 3 Boundary-Layer Thickness Ratios, $g=\delta^*/\delta$ and $H=\delta^*/\theta$, on the Flexible Plate and Sidewall Centerlines at Mach Numbers 2 through 5

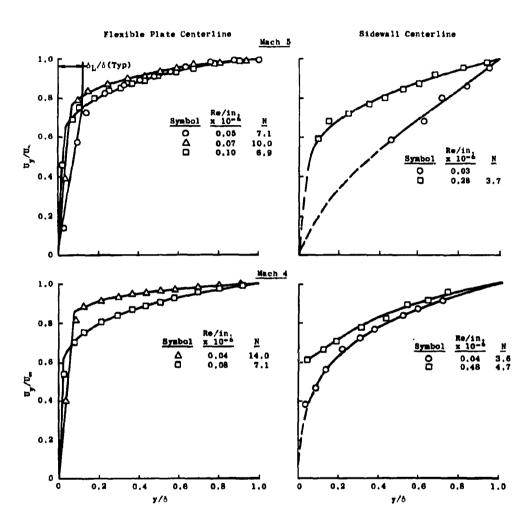


Fig. 4 Velocity Profiles on the Flexible Plate and Sidewall Centerlines at Mach Numbers 4 and 5

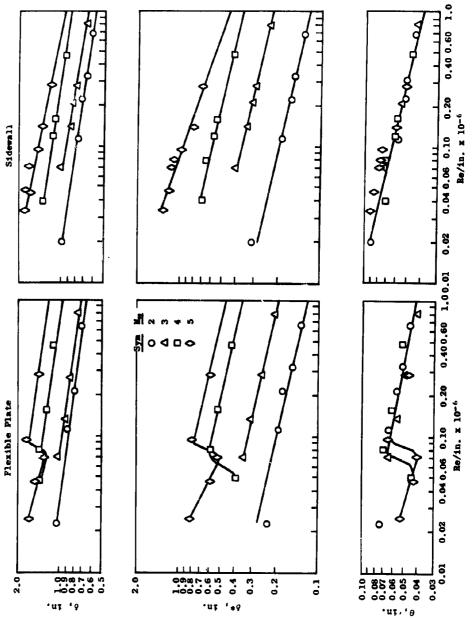


Fig. 5 Total, Displacement, and Momentum Thickness on the Flexible Plate and Sidewall Centerlines at Mach Numbers 2 through 5

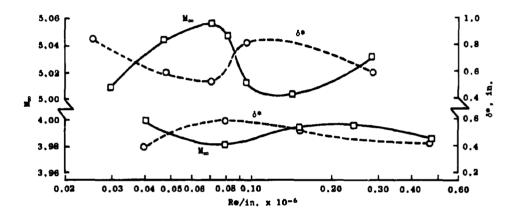


Fig. 6 Mach Number and Displacement Thickness Variation with Reynolds Number at Mach Numbers 4 and 5

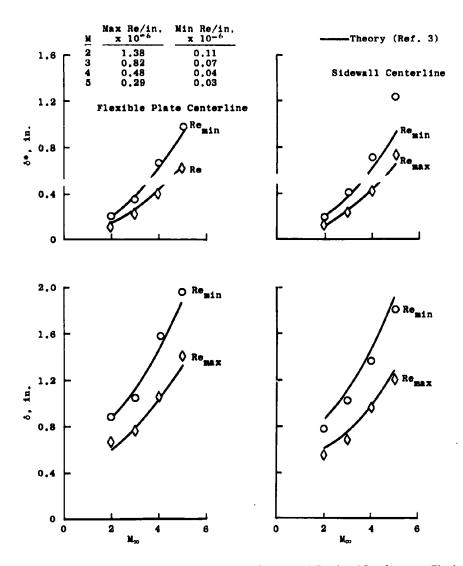


Fig. 7 Comparison between Experimental and Theoretical Values of Total and Displacement Thickness on the Flexible Plate and Sidewall Centerline at Mach Numbers 2 through 5

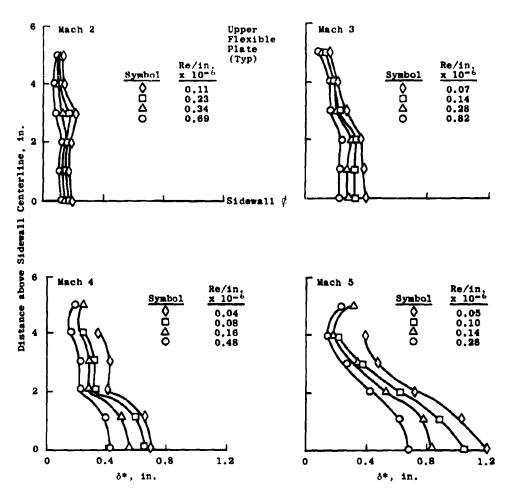


Fig. 8 Variation of the Sidewall Displacement Thickness between the Centerline and Upper Flexible Plate at Mach Numbers 2 through 5

| Symbol | Facility | Test Section | Ref. |
|----------------------------------------|--------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------|-----------------------------------------------|
| 00000000000000000000000000000000000000 | AEDC (VKF) AEDC (VKF) AEDC (PWT) JPL JPL NASA OAL DRL RAE UTIA NSL | 12" x 12" 40" x 40" 12" x 12" 20" x 20" 20" x 20" 3.84" x 10" 19" x 27.5" 1.45" x 1.45" 8' x 8' 5" x 7" 18" x 24" | 7 6 8 9 5 10 11 12 13 |

* $\overline{\delta^*}$ computed at aerodynamic exit plane.

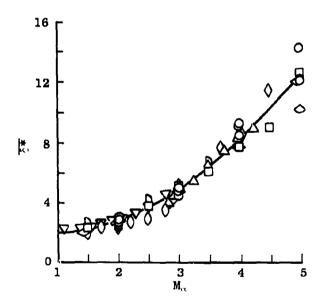


Fig. 9 Flaxible Plate Displacement Thickness Correlation at Mach Numbers 1.5 through 5